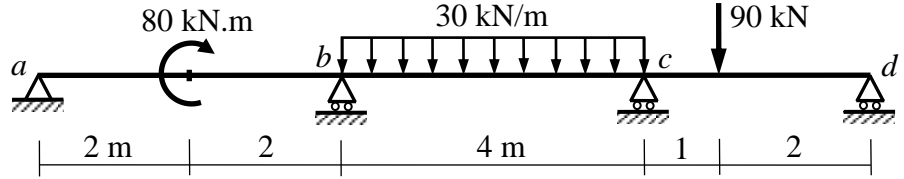


## Final Exam

Total Marks: 70

No. of Questions: 40 (Attempt all questions)

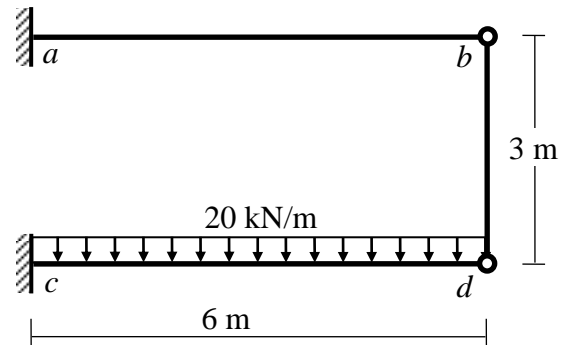
For the shown beam, use the **three-moment equation** to draw the shear force and the bending moment diagrams.



Choose the nearest answer.

- The shown beam has ... unknown moments at supports.  
(A) 1 (B) 2 (C) 3 (D) 4
- In  $M_o$ -diagram due to the given loads, the maximum moment in the span  $ab$  is:  
(A) 20 kN.m (B) 80 kN.m (C) 40 kN.m (D) 90 kN.m
- In  $M_o$ -diagram due to the given loads, the maximum moment in the span  $bc$  is:  
(A) 15 kN.m (B) 30 kN.m (C) 40 kN.m (D) 60 kN.m
- The elastic reaction at the support  $b$  from span  $ba$  ( $r_{ba}$ ) is:  
(A) zero (B) 13.33 (C) 20 (D) 40
- The elastic reaction at the support  $b$  from span  $bc$  ( $r_{bc}$ ) is:  
(A) 30 (B) 60 (C) 80 (D) 120
- The elastic reactions at the support  $c$  ( $r_{cb}$  &  $r_{cd}$ ) are:  
(A) 80 & 50 (B) 60 & 50 (C) 120 & 90 (D) 80 & 45
- The final moment at the support  $b$  is:  
(A) -22.7 kN.m (B) -25.4 kN.m (C) -30.3 kN.m (D) -49.2 kN.m
- The final moment at the support  $c$  is:  
(A) -25.4 kN.m (B) -49.2 kN.m (C) -55.2 kN.m (D) -42.1 kN.m
- The final maximum positive moment in the span  $ab$  is:  
(A) 47.3 kN.m (B) 72.2 kN.m (C) 28.7 kN.m (D) 51.4 kN.m
- The final shear force at  $a$  is:  
(A) zero (B) 12.2 kN (C) -25.7 kN (D) -36.4 kN
- The final shear force at  $d$  is:  
(A) -76.2 kN (B) -12.2 kN (C) -25.7 kN (D) -13.6 kN

For the shown frame, use the **consistent deformations (virtual work)** method to draw the bending moment diagram. Take the **main system by replacing the fixed support at C by hinged support**.  $EI$  is constant.

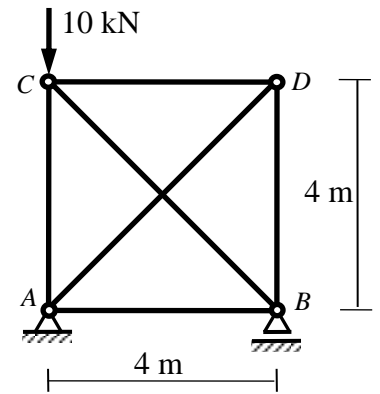


Choose the nearest answer.

- The moment at  $a$  in  $M_o$ -diagram due to the given loads is:  
(A) -900 kN.m (B) zero (C) -360 kN.m (D) -450 kN.m
- The moment at  $c$  in  $M_o$ -diagram due to the given loads is:  
(A) 20 kN.m (B) 120 kN.m (C) zero (D) 60 kN.m
- The value of the moment at  $a$  in  $M_1$ -diagram due to the moment redundant  $X_1 = 1$  kN.m at  $c$  is:  
(A) zero (B) 1 kN.m (C) 3 kN.m (D) 6 kN.m
- The value of the moment at  $c$  in  $M_1$ -diagram due to the moment redundant  $X_1 = 1$  kN.m at  $c$  is:  
(A) zero (B) 1 kN.m (C) 3 kN.m (D) 6 kN.m
- The value of the deflection  $\delta_{10}$  is:  
(A)  $900/EI$  (B)  $2250/EI$  (C)  $200/EI$  (D)  $400/3EI$
- The value of the deflection  $\delta_{11}$  is:  
(A)  $16/EI$  (B)  $2/EI$  (C)  $8/EI$  (D)  $4/EI$
- The value of the final moment reaction at the fixed support  $c$  ( $X_1 = M_c$ ) is:  
(A) 225 kN.m (B) 562.5 kN.m (C) 107.5 kN.m (D) 82.3 kN.m
- The value of the final moment at  $a$  is:  
(A) 270 kN.m (B) 180 kN.m (C) 337.5 kN.m (D) 135 kN.m
- The value of the final moment at  $b$  is:  
(A) 1 kN.m (B) 4 kN.m (C) 135 kN.m (D) zero

**Please turn over**

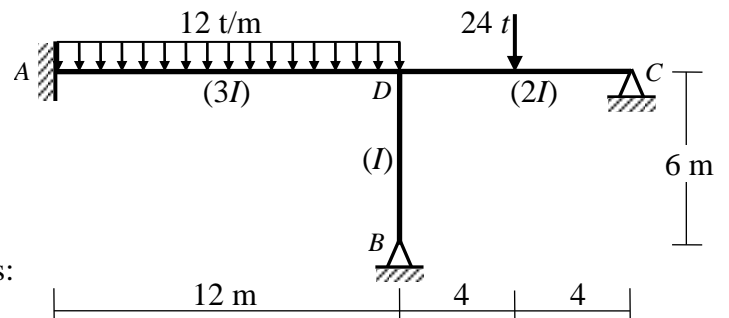
For the shown truss, use the **consistent deformations (virtual work)** method to determine the forces in the members. **Take the main system by removing the member BC.** Assume  $EA$  is constant for all members.



**Choose the nearest answer.**

21. The vertical reaction at the hinged support A due to the given loads ( $N_o$ ) is:  
 (A) zero (B) 5 kN  $\uparrow$  (C) 20 N  $\uparrow$  (D) 10 kN  $\uparrow$
22. The force in member AC due to the given loads ( $N_o$ ) is:  
 (A) 10 kN C (B) zero (C) 5 kN C (D) 10 kN T
23. The value of the force in member AC due to force  $X_I=1$  kN in member CB is:  
 (A) zero (B) 1 kN (C) 0.71 kN (D) 1.41 kN
24. The value of the deflection  $\delta_{10}$  is:  
 (A) 28.3/EA (B) 83.2/EA (C) 0.54/EA (D) 13.2/EA
25. The final force in member AC is:  
 (A) 8.96 C (B) 7.28 kN C (C) 6.71 kN C (D) 7.91 kN T
26. The final force in member AB is:  
 (A) 1 C (B) 1 T (C) zero (D) 0.71 kN C

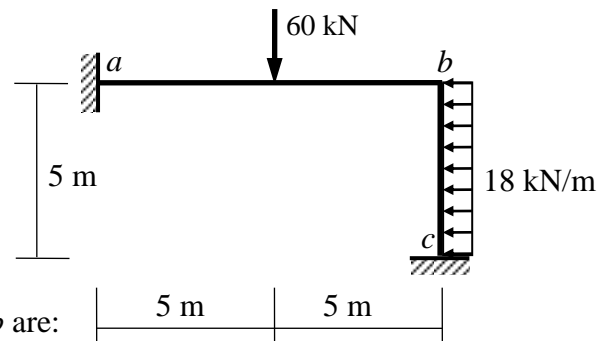
For the shown frame, use **the slope deflection method** to draw the bending moment diagram. Note that  $E$  is constant and the relative moments of inertia are given between brackets. Neglect axial deformation.



**Choose the nearest answer.**

27. The value of the fixed end moments of span AD is:  
 (A) 12 m.t (B) 9 m.t (C) 36 m.t (D) 144 m.t
28. The value of the fixed end moment of span DC at D is:  
 (A) 12 m.t (B) 9 m.t (C) 144 m.t (D) 36 m.t
29. The value of the fixed end moment of column DB at D is:  
 (A) zero (B) 6 m.t (C) 12 m.t (D) 16 m.t
30. The value of the unknown displacement  $\theta_D$  is:  
 (A) 48/EI (B) 3/EI (C) 300/EI (D) 183/EI
31. The value of the final moment at A is:  
 (A) 12 m.t (B) 3 m.t (C) 168 m.t (D) 48 m.t
32. The final maximum negative moment in the span DC is:  
 (A) -6 m.t (B) -12 m.t (C) -72 m.t (D) -27 m.t
33. The value of the final maximum moment in the column BD is:  
 (A) zero (B) 9 m.t (C) 24 m.t (D) 90 m.t

For the shown frame, use **the moment distribution method** to draw the bending moment diagram.  $EI$  is constant.



**Choose the nearest answer.**

34. The value of the fixed end moment of span ab at b is:  
 (A) 150 kN.m (B) 60 kN.m (C) 75 kN.m (D) 500 kN.m
35. The value of the fixed end moment of column bc at b is:  
 (A) 11.25 kN.m (B) 18 kN.m (C) 56.25 kN.m (D) 37.5 kN.m
36. The distribution factors of the excess bending moment at joint b are:  
 (A) 4/7 & 3/7 (B) 1/3 & 2/3 (C) 10/3 & 5/3 (D) 1/2 & 1/2
37. The final bending moment at a is:  
 (A) -81.25 kN.m (B) -62.25 kN.m (C) -25.25 kN.m (D) -75.25 kN.m
38. The final bending moment at b is:  
 (A) -32.5 kN.m (B) -12.8 kN.m (C) -37.5 kN.m (D) -62.5 kN.m
39. The final bending moment at c is:  
 (A) -51.2 kN.m (B) -25 kN.m (C) -96 kN.m (D) 20 kN.m
40. The final bending moment at the middle of column bc is:  
 (A) 25 kN.m (B) 12.5 kN.m (C) 37.5 kN.m (D) -62.5 kN.m

With my best wishes

**Dr. M. Abdel-Kader**