

Answer of Final Exam

Total Marks: **90**

No. of Questions: **3** (Attempt all questions)

Question (1): (30 Marks)

Entire (Total) Structure

$$+\circlearrowleft \sum M_A = 0: \quad B_x(4) + 50(2) - 60(7) - 40(2) = 0$$

$$\therefore B_x = +100 \rightarrow$$

$$\boxed{B_x = 100 \text{ kN} \rightarrow}$$

$$+\rightarrow \sum F_x = 0: \quad 50 + 100 - A_x = 0$$

$$\therefore A_x = +150 \leftarrow$$

$$\boxed{A_x = 150 \text{ kN} \leftarrow}$$

Part BC:

$$+\circlearrowleft \sum M_C = 0: \quad 50(2) + 100(4) - B_y(4) = 0$$

$$\therefore B_y = 125 \uparrow$$

$$\boxed{B_y = 125 \text{ kN} \uparrow}$$

Entire Structure

$$+\uparrow \sum F_y = 0: \quad A_y + 125 - 60 - 40 = 0$$

$$\therefore A_y = -25 \uparrow$$

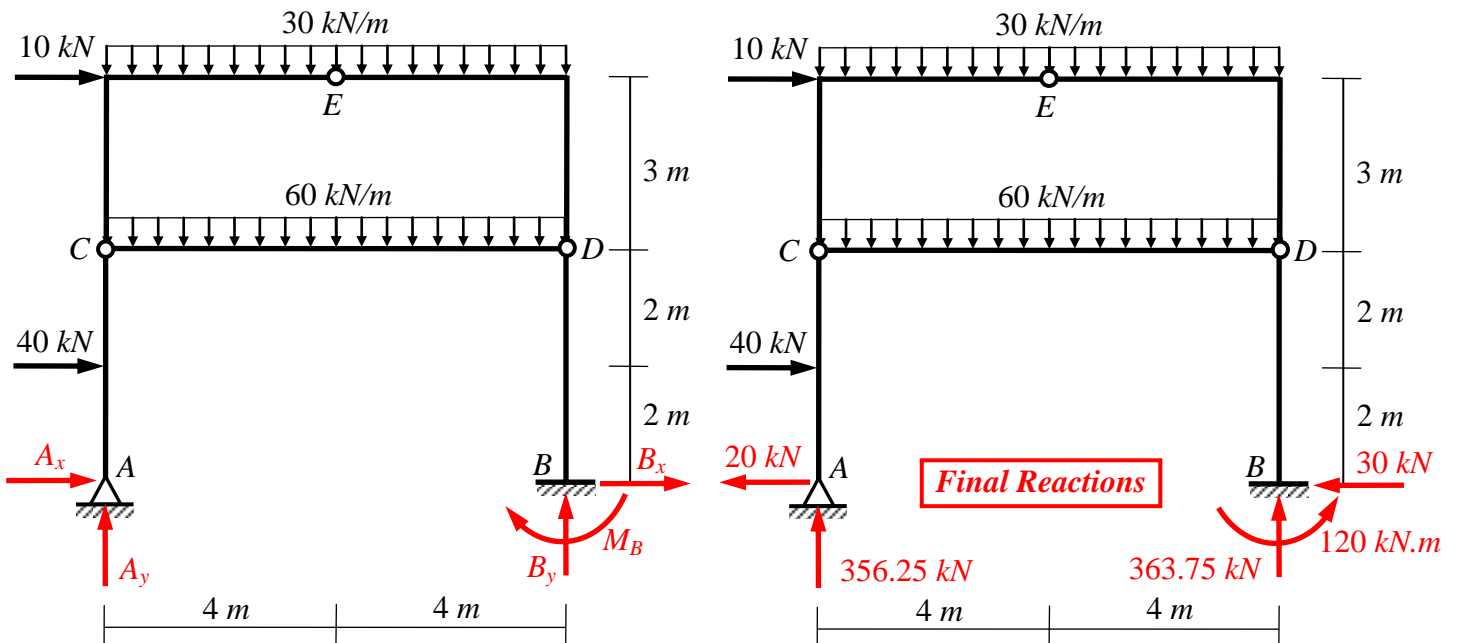
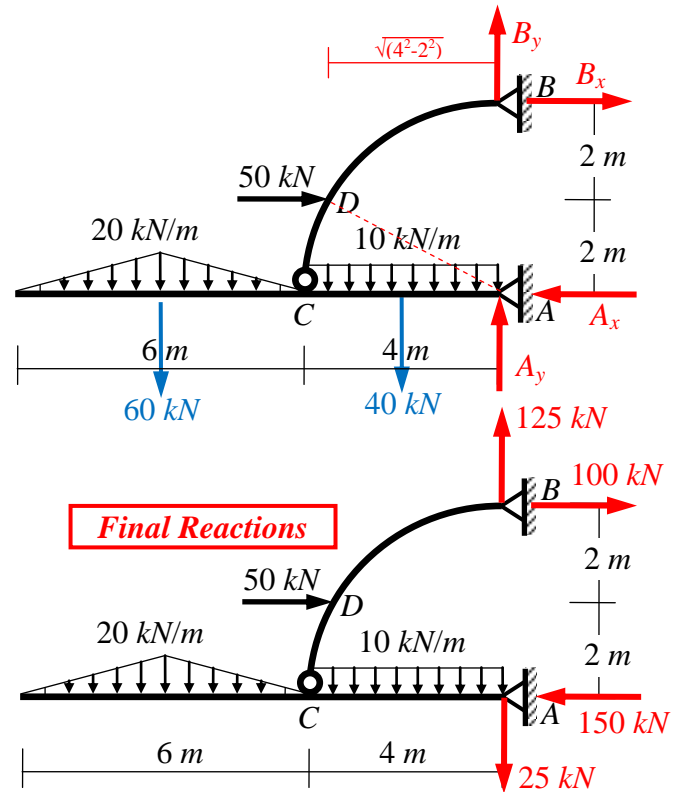
$$\boxed{A_y = 25 \text{ kN} \downarrow}$$

Moment at D

$$= 125(\sqrt{4^2 - 2^2}) - 100(2)$$

$$= 233 \text{ kN.m} \curvearrowright$$

$$\boxed{M_D = 233 \text{ kN.m} \curvearrowright}$$



Part AC:

$$+\circlearrowleft \sum M_C = 0 \quad -40(2) - A_x(4) = 0$$

$$\boxed{A_x = 20 \text{ kN} \leftarrow}$$

Entire (Total) Frame:

$$+\rightarrow \sum F_x = 0 \quad -20 + 40 + 10 + B_x = 0$$

$$\boxed{B_x = 30 \text{ kN} \leftarrow}$$

Part BD:

$$+\circlearrowleft \sum M_D = 0 \quad 30(4) + M_B = 0$$

$$\boxed{M_B = 120 \text{ kN.m} \curvearrowright}$$

Entire (Total) Frame:

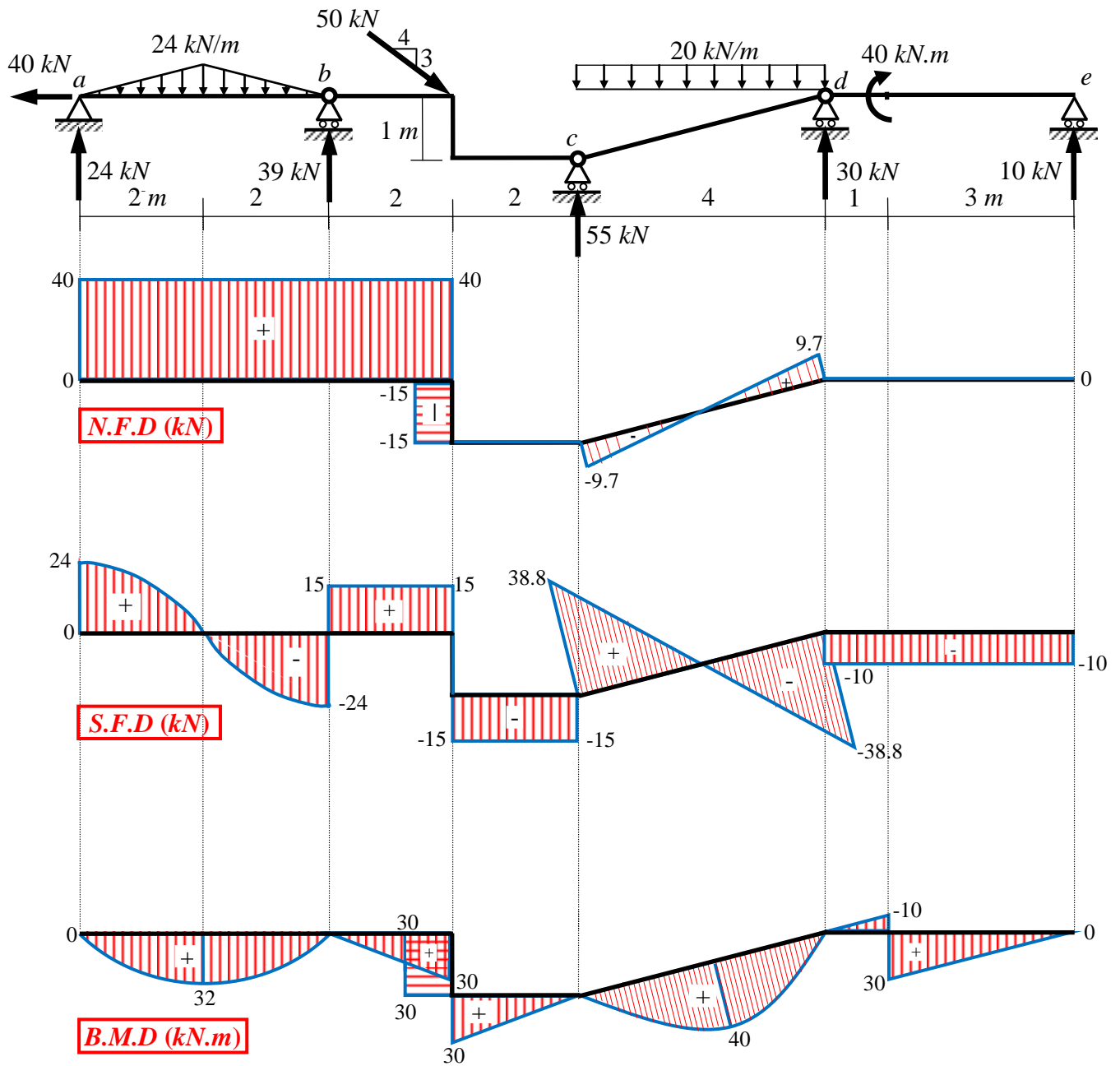
$$+\circlearrowleft \sum M_A = 0 \quad 40(2) + 10(7) + (4) - 120 - B_y(8) = 0$$

$$\boxed{B_y = 363.75 \text{ kN} \uparrow}$$

$$+\uparrow \sum F_y = 0 \quad A_y - 30 \times 8 - 60 \times 8 + 363.75 = 0$$

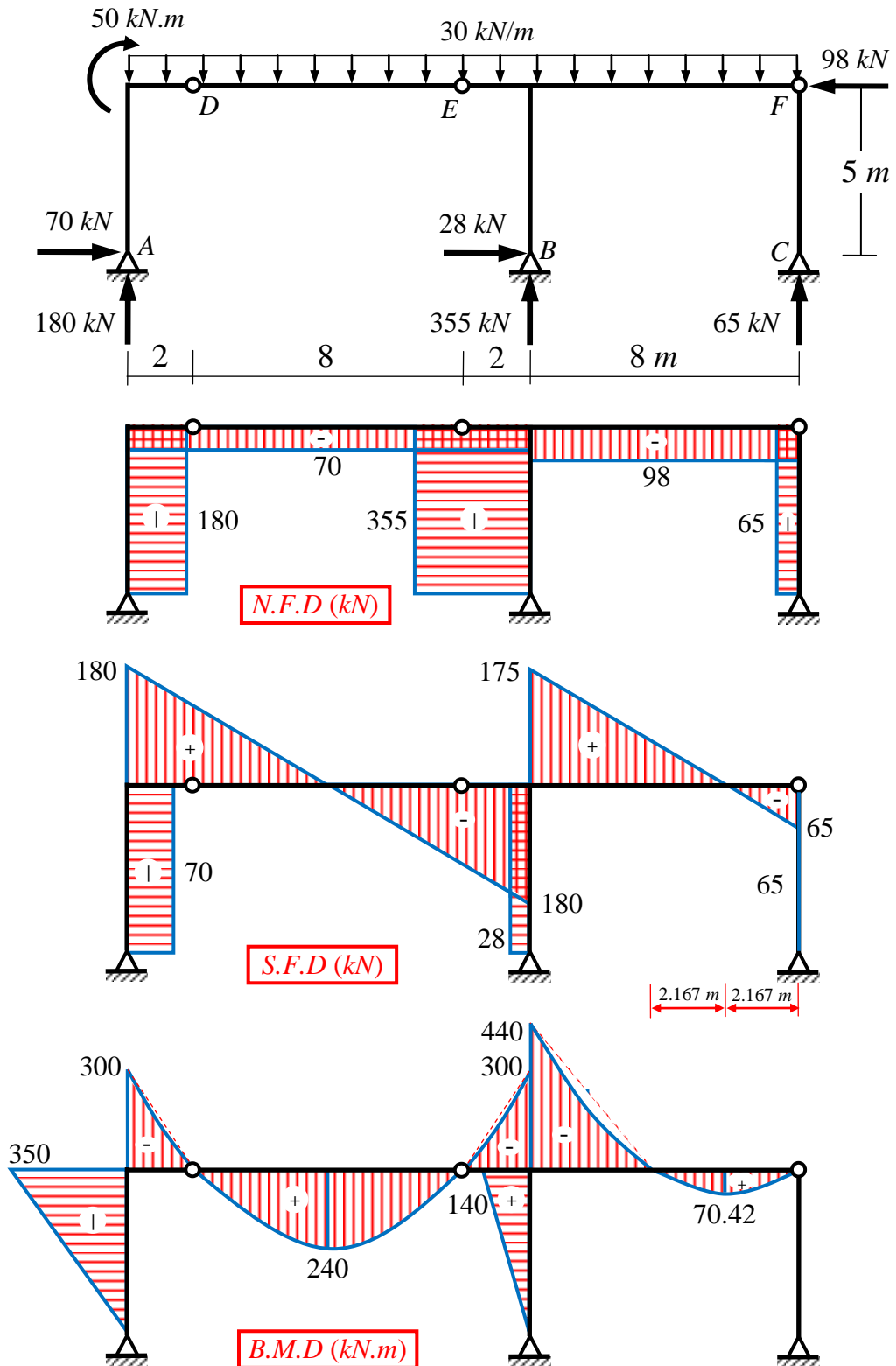
$$\boxed{A_y = 356.25 \text{ kN} \uparrow}$$

Question (2a): (15 Marks)



With my best wishes
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Question (2b): (15 Marks)



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Question (3): (30 Marks)

(i) Zero-force members are 7 and 11.

7 and **11**

(ii) Method of joints:

Joint d:

$$+\rightarrow \sum F_x = 5 + F_2/\sqrt{2} = 0$$

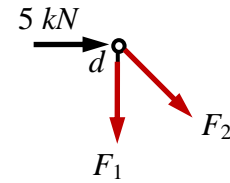
$$\therefore F_2 = -5\sqrt{2} = -7.07$$

$F_2 = 7.07 \text{ kN Compression}$

$$+\uparrow \sum F_y = -F_1 - F_2/\sqrt{2} = -F_1 - (-5\sqrt{2})/\sqrt{2} = -F_1 + 5 = 0$$

$$\therefore F_1 = +5$$

$F_1 = 5 \text{ kN Tension}$



Joint d

Joint c:

$$+\rightarrow \sum F_x = 0 \quad \therefore F_3 = -10$$

$F_3 = 10 \text{ kN Compression}$

(iii) Method of sections:

$$- +\cup \sum M_b = 0$$

$$10(4) + 5(8) + 5(4) + F_6(4) = 0$$

$$\therefore F_6 = -25 \quad \mathbf{F_6 = 25 \text{ kN Compression}}$$

$$- +\cup \sum M_e = 0$$

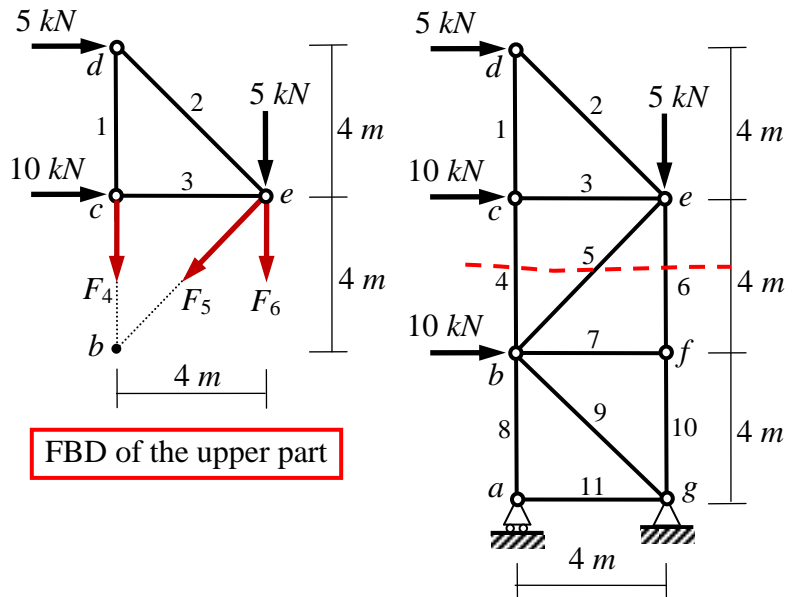
$$5(4) - F_4(4) = 0$$

$$\therefore F_4 = 5 \quad \mathbf{F_4 = 5 \text{ kN Tension}}$$

$$- +\rightarrow \sum F_x = 5 + 10 - F_5/\sqrt{2} = 0$$

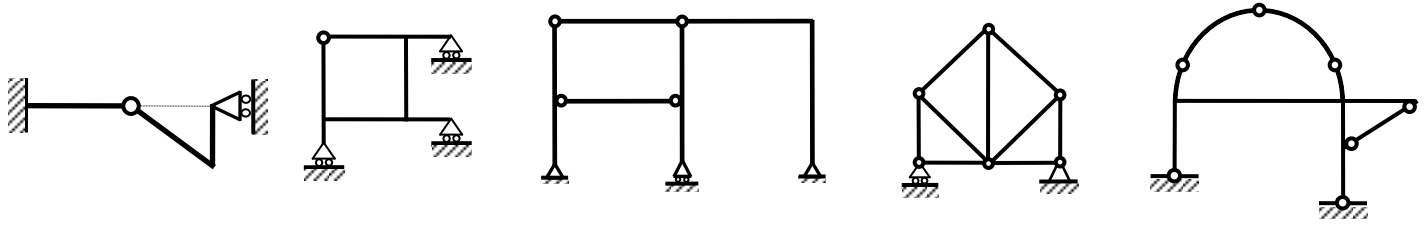
$$\therefore F_5 = 15\sqrt{2} = 21.2$$

$F_5 = 21.2 \text{ kN Tension}$



FBD of the upper part

(b)



Unstable

Unstable

Stable + Stat. Det.

Stable + Stat. Det.

Stable + Stat. Indet. to the 2nd degree.

(1)

(2)

(3)

(4)

(5)

With my best wishes

Dr. M. Abdel-Kader