

### Mid-Term Exam

Total Marks: 20

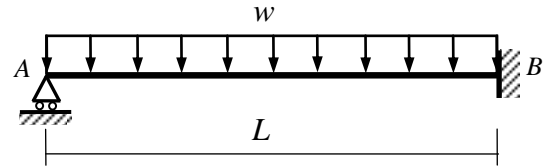
No. of Questions: 2

Student Name:

Code:

#### Question (1): (10 Marks)

For the shown beam, using the **three-moment equation**, draw the shear force and bending moment diagrams due to the applied load.



#### Solution:

Apply 3-M eqn at B

$$2M_B(L) + M_A(L) = -6r_B = -\frac{wL^3}{4}$$

$$2M_B + 0 = -\frac{wL^2}{4}$$

$$\Rightarrow M_B = \boxed{-\frac{wL^2}{8}}$$

$$M_{max} = \frac{3}{8}wL\left(\frac{3}{8}L\right) - \frac{w}{2}\left(\frac{3}{8}L\right)^2$$

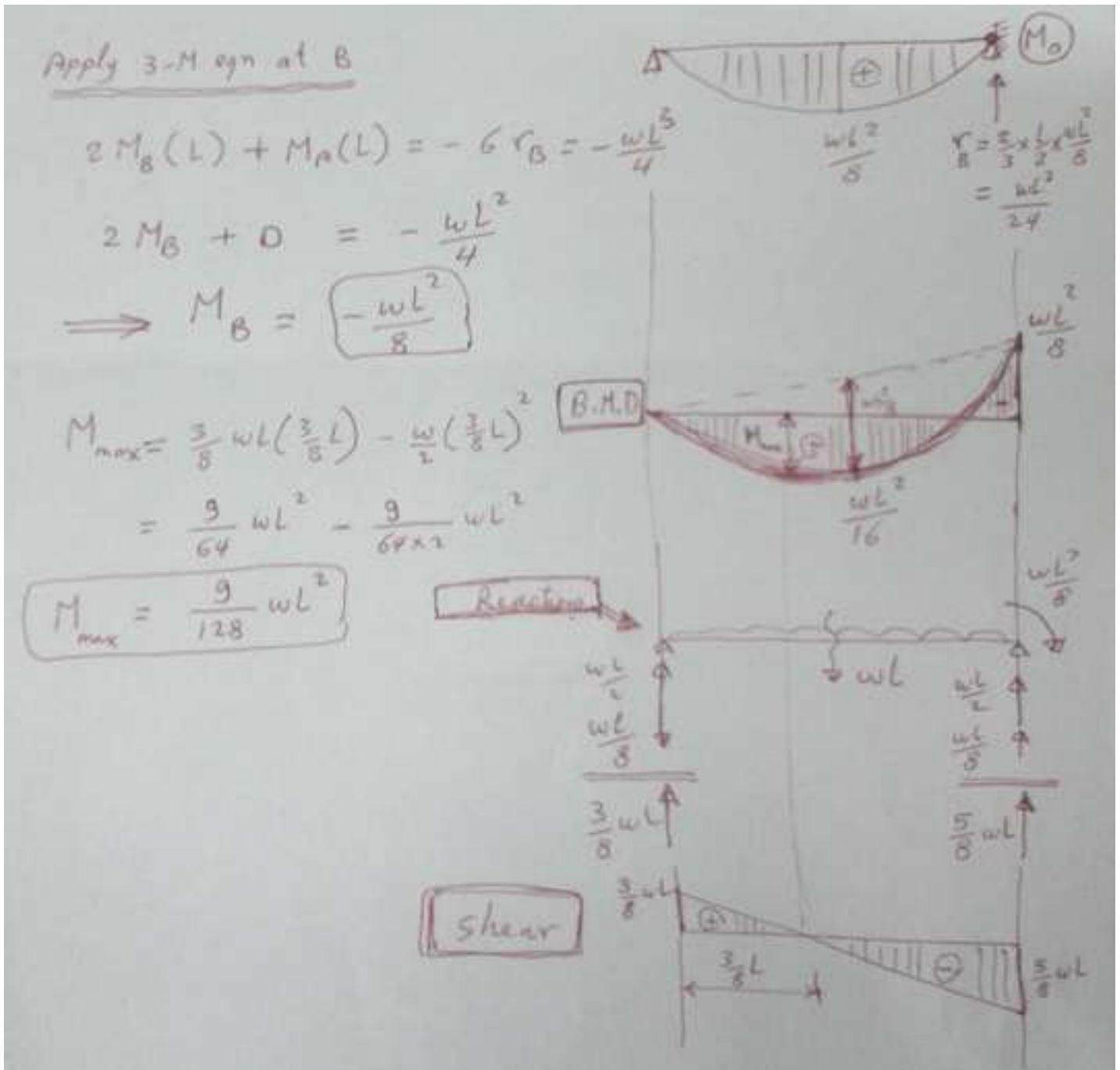
$$= \frac{9}{64}wL^2 - \frac{9}{64 \times 2}wL^2$$

$$M_{max} = \boxed{\frac{9}{128}wL^2}$$

**B.M.D**

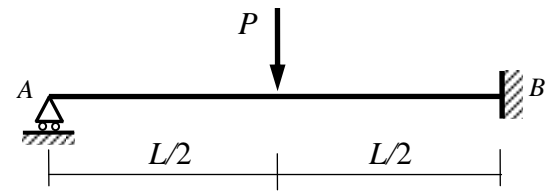
**Reactions**

**Shear**



**Question (2): (10 Marks)**

For the shown beam, using the **Consistent Deformations (Virtual Work)** method, draw the bending moment diagram due to the applied load.



**Solution:**

$$\delta_{10} = \int \frac{M_0 M_1}{EI} dl$$
$$= \frac{1}{EI} \left[ \left( \frac{1}{2} \times L \times \frac{PL}{4} \right) \left( -\frac{1}{2} \right) \right]$$
$$= \boxed{\frac{-PL^2}{16EI}}$$

$$\delta_{10} = \int \frac{M_1 M_1}{EI} dl$$
$$= \frac{1}{EI} \left[ \left( \frac{1}{2} \times L \times 1 \right) \left( \frac{2}{3} \times 1 \right) \right]$$
$$= \boxed{\frac{L}{3EI}}$$

$$\delta_{10} + X_1 \delta_{11} = 0$$
$$X_1 = - \frac{\delta_{10}}{\delta_{11}} = \boxed{\frac{3}{16} PL}$$

**Main system**  $(M_0)$

$M_1$

**B.M.D**