

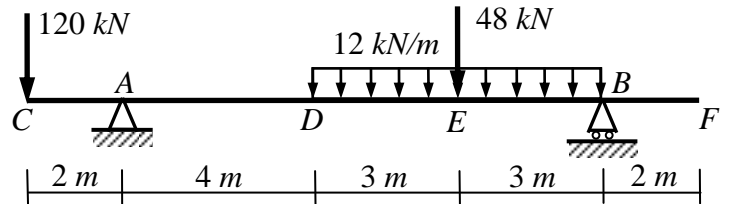
## Final Exam

- Attempt all questions.
- The Exam consists of **5** questions in **1** page.
- Maximum grade is **60 Marks**

### Question (1): (12 Marks)

For the shown beam, using the **double integration method**, determine: the deflections at *C*, *D* and *F* and the slope at *C*. Also, sketch the elastic curve of the beam.

$$EI = 2 \times 10^5 \text{ kN.m}^2$$



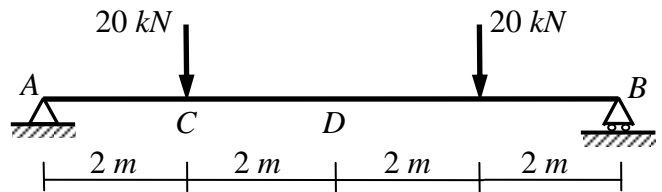
### Question (2): (12 Marks)

For the shown beam, using the **moment-area method**, determine:

- (a) the slope at *A*
- (b) the deflection at *D*
- (c) the deflection at *C*

and sketch the elastic curve of the beam.

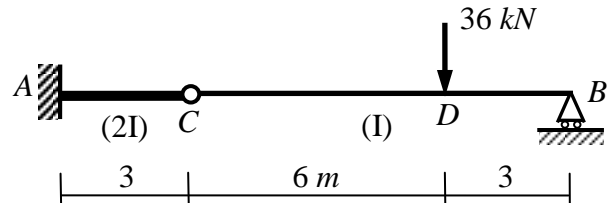
$$E = 400 \text{ GPa} \text{ and } I = 1300 \text{ cm}^4$$



### Question (3): (12 Marks)

For the shown beam of variable cross-section (the relative moments of inertia are given between brackets), using the **conjugate beam method**, determine the slope at *B* and the deflections at *C* and *D*. Also, sketch the elastic curve of the beam.

$$EI = 20 \times 10^3 \text{ kN.m}^2$$

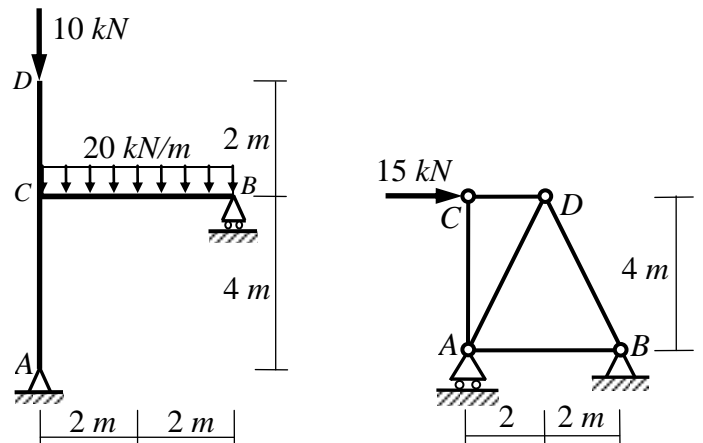


### Question (4): (12 Marks)

For the shown frame and truss, using the **virtual work method**, determine the horizontal displacements at *D* ( $\delta_{Dh}$ ).

For the frame,  $EI = 50 \times 10^3 \text{ kN.m}^2$ .

For the truss, assume that all members have the same axial rigidity  $EA = 10000 \text{ kN}$ .

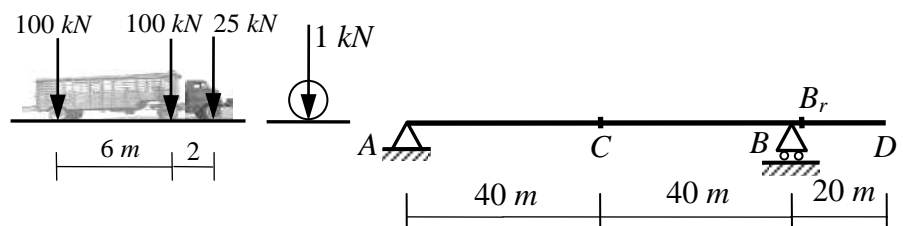


### Question (5): (12 Marks)

For the shown beam, draw the influence lines for:

- (a) the reactions  $A_y$  and  $B_r$ ,
- (b) the shear forces at *C* and  $B_r$ ,
- (c) the bending moment at *C*

Also, determine the maximum positive moment at *C* caused by the shown moving truck.



With my best wishes

**Dr. M. Abdel-Kader**