

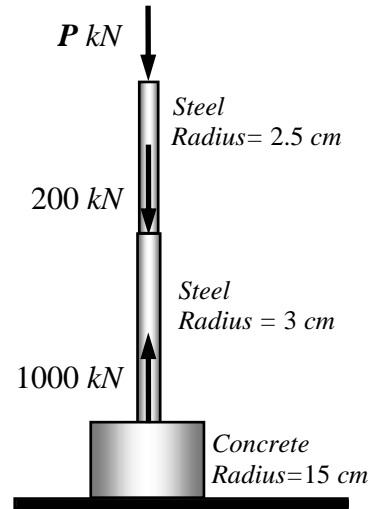
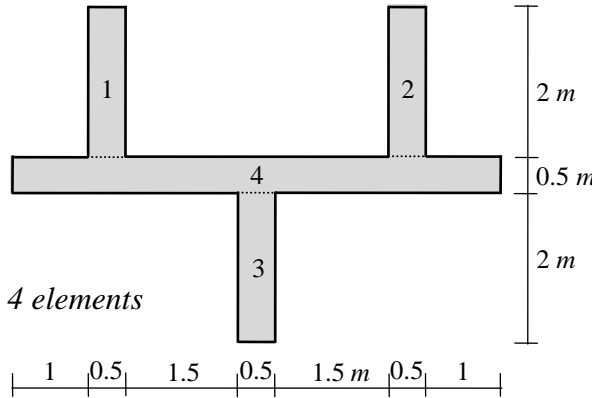
Total Marks: **90**

No. of Questions: **3** (Attempt all questions)

**Question (1): (30 Marks)**

- (a) For the shown cross-section, determine the following:
- The location of the centroid.
  - The moments of inertia about the centroidal axes.
  - The polar moment of inertia.
  - The radii of gyration ( $r_x$  &  $r_y$ ).

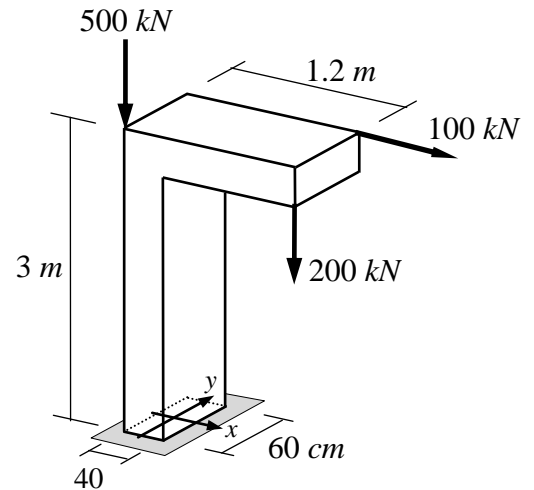
**Note:** Divide the cross-section to 4 elements as shown on the figure.



- (b) A column of variable circular cross-section is subjected to axial loads as shown. Determine the safe range of  $P$ .

**Given Data:**

- For **Steel:** Allowable compressive and tensile stresses =  $140 \text{ MPa}$   
 For **Concrete:** Allowable compressive stress =  $80 \text{ MPa}$   
 Allowable tensile stress =  $10 \text{ MPa}$



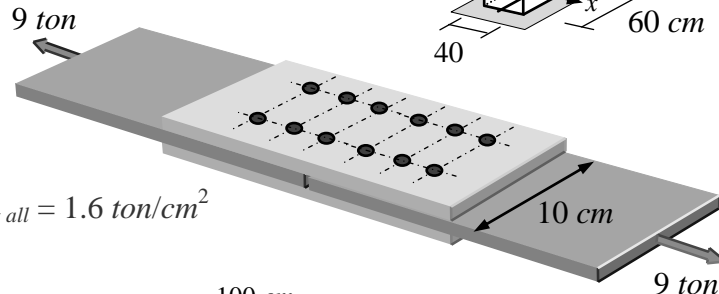
**Question (2): (30 Marks)**

- (a) For the shown column, draw the normal stress distribution at the base section ( $40 \text{ cm} \times 60 \text{ cm}$ ) and calculate the maximum normal stresses. Neglect the column weight.

- (b) For the shown bolted butt joint, determine the safe diameter of bolts. The width of plates is  $10 \text{ cm}$ , and the thickness of plates is  $12 \text{ mm}$ . The allowable stresses are as follows:

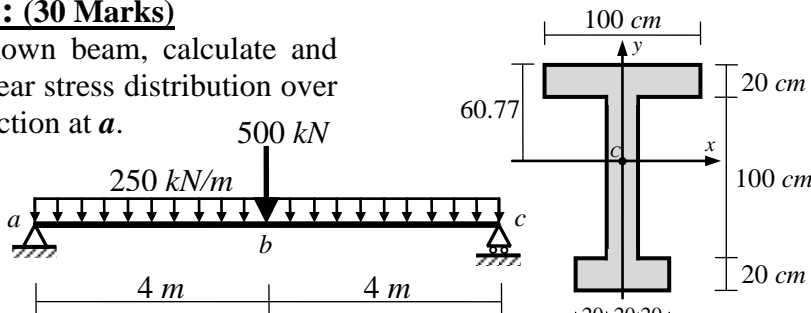
**Bolts:**  $\tau_{all} = 1.1 \text{ ton/cm}^2$ ,

**Plates:**  $\sigma_{t all} = 1.4 \text{ ton/cm}^2$  and  $\sigma_{bearing all} = 1.6 \text{ ton/cm}^2$



**Question (3): (30 Marks)**

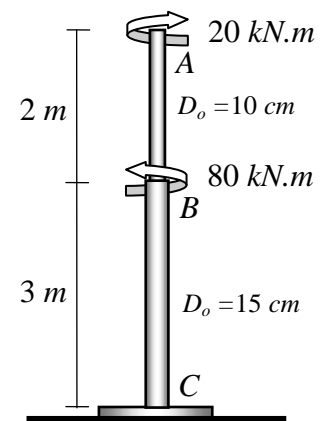
- (a) For the shown beam, calculate and draw the shear stress distribution over the cross-section at  $a$ .



**Cross-section of the beam**

- (b) A column of two tubes must resist torques as shown. The tubes have outside diameters of  $10 \text{ cm}$  and  $15 \text{ cm}$  and a thickness of  $10 \text{ mm}$ .

- Draw the twisting moment diagram.
- Determine the maximum shear stress  $\tau_{max}$  in the two tubes.
- Determine the relative angle of twist  $\phi$  between  $A$  and  $C$ , where  $G = 30 \text{ GPa}$ .



With best wishes

**Dr. M. Abdel-Kader**