

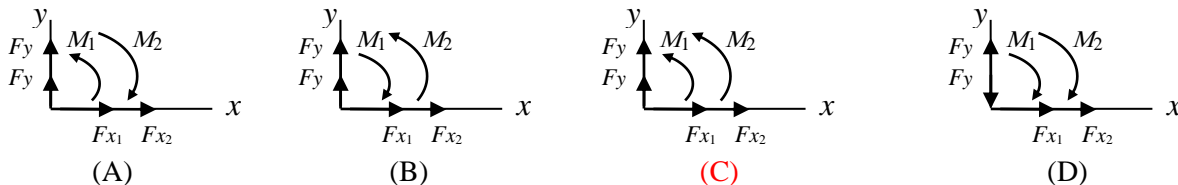
Final Exam

Total Marks: 75

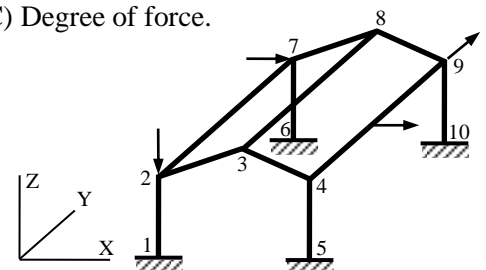
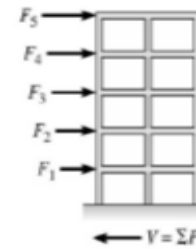
No. of Questions: 50 (Attempt all questions)

Choose the nearest answer.

- Stiffness is the property of an element which is defined as:
(A) Displacement per unit area. (B) Displacement per unit force. (C) Force per unit force.
(D) Force per unit displacement.
- For plane frame element 1-2 (connecting joints 1 and 2), the positive sign of forces (forces and moments) is:



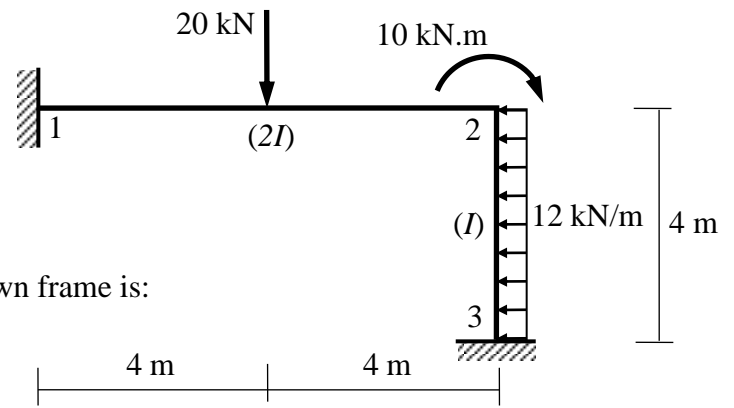
- One of the assumptions that the stiffness method is based on to analyze plane frames is:
(A) Members will behave in non-linear and plastic manner.
(B) Members (beams and columns) are straight with constant properties between joints.
(C) Applied loads will act out of the structure plane.
- In SAP, loads and properties of material are:
(A) Fixed data. (B) Output data. **(C) Input data.** (D) Results of the analysis.
- In SAP, the must be defined for (1D) plane frame elements.
(A) Areas (B) Thicknesses **(C) Sections** (D) Colors
- The horizontal forces applied on the shown frame is called load.
(A) Earth pressure **(B) Earthquake** (C) Settlement (D) Hydrostatic
- In SAP, the internal forces are:
(A) Fixed data. (B) Input data. (C) Given data. **(D) Output data.**
- In SAP, self-weight loading always acts in the ... direction.
(A) X (B) Y (C) -Y **(D) -Z**
- Wind load applied over the height of high-rise buildings is assumed:
(A) Constant. (B) 1000 kN/m. **(C) Perpendicular to the surface.** (D) Parallel to the surface.
- When the material properties are independent of the coordinates, the material is:
(A) Isotropic. (B) Non-linear. (C) Plastic. **(D) Homogeneous.**
- The responsibility of the analytical model results lies on:
(A) The company developed the software. (B) The structural designer who developed the software.
(C) The structural designer who used the software. (D) The computer used.
- The abbreviation "CAD" means:
(A) Common Analysis Data. **(B) Computer-Aided Design.** (C) Calculation And Design. (D) Computer And Data.
- The abbreviation "DOF" means:
(A) Possible translations at nodes. (B) Possible rotations at nodes. (C) Degree of force.
(D) Possible translations and rotations at nodes.
- The number of non-zero DOF for the shown space frame is:
(A) 60 (B) 30 **(C) 36** (D) 18
- The number of non-zero DOF per node 1 in the shown space frame is:
(A) Zero (B) 6 (C) 2 (D) 3
- The number of non-zero DOF per node 2 in the shown space frame is:
(A) Zero (B) 3 (C) 4 **(D) 6**
- If the axial deformation is neglected, the number of non-zero DOF per node 2 in the shown space frame is:
(A) 4 (B) 3 **(C) 5** (D) 2
- When there are loads between the nodes, the equilibrium equation of a plane frame is $\{F\} = [K]\{\Delta\} + \{F^f\}$ where;
(A) $\{F\}$ is the nodal forces. (B) $\{F^f\}$ is the nodal displacements. (C) $[F^f]$ is the element stiffness matrix.
(D) $\{\Delta\}$ is the nodal forces.
- In 2D Analysis, can be used.
(A) only 2D elements. (B) 1D, 2D and 3D elements. (C) 2D and 3D elements **(D) 1D and 2D elements.**
- Structures that cannot be modeled with the frame element are:
(A) Space frames. (B) Space trusses. **(C) Flat slabs.** (D) Plane frames.



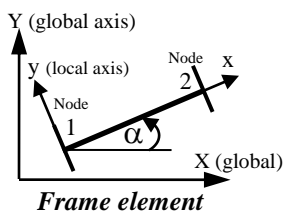
Please turn over

For the shown loaded plane frame with variable moment of inertia, use **the stiffness method** and **neglect axial deformation**:

Choose the nearest answer.



21. The shown frame has ... nodes.
(A) 1 (B) 2 (C) 3 (D) 4
22. The least number of elements to be taken for the shown frame is:
(A) 1 (B) 2 (C) 3 (D) 4
23. By neglecting axial deformation, the number of the non-zero DOF for the shown frame becomes:
(A) Zero (B) 1 (C) 2 (D) 3
24. The terms (coefficients) of the force vector $\{F\}$ of the shown frame are:
(A) $X_1, Y_1, M_1, 0, 0, -10, X_3, Y_3, M_3$ (B) $X_1, Y_1, M_1, 0, 20, 0, X_3, Y_3, M_3$ (C) $X_1, Y_1, -20, 10, 20, 0, X_3, Y_3, M_1$
25. The terms (coefficients) of the displacement vector $\{\Delta\}$ of the shown frame are:
(A) $0, 0, 0, u_2, v_2, \theta_2, 0, 0, 0$ (B) $0, 0, 0, 0, 0, \theta_2, 0, 0, 0$ (C) $0, 0, 0, \theta_2, 0, 0$ (D) $0, 0, \theta_1, 0, 0, \theta_2, 0, 0, \theta_3$
26. The terms (coefficients) of the fixed end solution of element 1 (nodes 1 & 2) are:
(A) $0, 10, 20, 0, 10, -20$ (B) $0, 20, 10, 20, 10, -20$ (C) $10, 0, 20, 10, 0, -20$ (D) $0, 0, 20, 0, 0, -20$
27. The properties of element 1 (nodes 1 & 2) are.
(A) $\alpha = 0, \lambda = 1, \mu = 0$ and $L=8$ m (B) $\alpha = 0, \lambda = 1, \mu = 0$ and $L=4$ m (C) $\alpha = 0, \lambda = 0, \mu = 1$ and $L=8$ m
28. The terms (coefficients) of the sixth column of the stiffness matrix of element 1 $[K^1]$ are:
(A) $0, 3EI/16, EI/2, 0, -3EI/16, EI$ (B) $0, 0, EI/2, 0, -3EI/6, EI$ (C) $0, 0, EI/2, 0, -3EI, EI$
29. The rotation angle θ_2 at node 2 is:
(A) $-800/EI$ (B) $-30/2EI$ (C) $-3/EI$ (D) $-40/3EI$
30. The final bending moment at node 1 is:
(A) -1.5 kN.m (B) 8.0 kN.m (C) -72.5 kN.m (D) -18.5 kN.m
31. The final bending moments at node 2 are:
(A) 40 and 30 kN.m (B) -7 and -20 kN.m (C) -3 and -13 kN.m (D) -23 and -13 kN.m
32. The final bending moment at node 3 is:
(A) -17.5 kN.m (B) -17.5 kN.cm (C) -17.5 N.m (D) -17.5 kN.mm
33. The final bending moment at the middle of element 1 (nodes 1 & 2) is:
(A) 80.2 kN.m (B) 70.6 kN.m (C) 19.25 kN.m (D) 2.25 kN.m
34. The final bending moment at the middle of element 2 (nodes 2 & 3) is:
(A) zero (B) 70.6 kN.m (C) 18.5 kN.m (D) 8.75 kN.m
35. The final vertical reaction at node 1 is:
(A) 20.7 kN (B) 9.4 kN (C) 0.5 kN (D) 80.5 kN



$$[K_e] = \begin{bmatrix} \left(\frac{EA}{L} \lambda^2 + \frac{12EI}{L^3} \mu^2 \right) & \left(\frac{EA}{L} \mu \lambda - \frac{12EI}{L^3} \mu \lambda \right) & -\frac{6EI}{L^2} \mu & \left(-\frac{EA}{L} \lambda^2 - \frac{12EI}{L^3} \mu^2 \right) & \left(-\frac{EA}{L} \mu \lambda + \frac{12EI}{L^3} \mu \lambda \right) & -\frac{6EI}{L^2} \mu \\ \left(\frac{EA}{L} \mu \lambda - \frac{12EI}{L^3} \mu \lambda \right) & \left(\frac{EA}{L} \mu^2 + \frac{12EI}{L^3} \lambda^2 \right) & \frac{6EI}{L^2} \lambda & \left(-\frac{EA}{L} \mu \lambda + \frac{12EI}{L^3} \mu \lambda \right) & \left(-\frac{EA}{L} \mu^2 - \frac{12EI}{L^3} \lambda^2 \right) & \frac{6EI}{L^2} \lambda \\ -\frac{6EI}{L^2} \mu & \frac{6EI}{L^2} \lambda & \frac{4EI}{L} & \frac{6EI}{L^2} \mu & -\frac{6EI}{L^2} \lambda & \frac{2EI}{L} \\ \left(-\frac{EA}{L} \lambda^2 - \frac{12EI}{L^3} \mu^2 \right) & \left(-\frac{EA}{L} \mu \lambda + \frac{12EI}{L^3} \mu \lambda \right) & \frac{6EI}{L^2} \mu & \left(\frac{EA}{L} \lambda^2 + \frac{12EI}{L^3} \mu^2 \right) & \left(\frac{EA}{L} \mu \lambda - \frac{12EI}{L^3} \mu \lambda \right) & \frac{6EI}{L^2} \mu \\ \left(-\frac{EA}{L} \mu \lambda + \frac{12EI}{L^3} \mu \lambda \right) & \left(-\frac{EA}{L} \mu^2 - \frac{12EI}{L^3} \lambda^2 \right) & -\frac{6EI}{L^2} \lambda & \left(\frac{EA}{L} \mu \lambda - \frac{12EI}{L^3} \mu \lambda \right) & \left(\frac{EA}{L} \mu^2 + \frac{12EI}{L^3} \lambda^2 \right) & -\frac{6EI}{L^2} \lambda \\ -\frac{6EI}{L^2} \mu & \frac{6EI}{L^2} \lambda & \frac{2EI}{L} & \frac{6EI}{L^2} \mu & -\frac{6EI}{L^2} \lambda & \frac{4EI}{L} \end{bmatrix}$$

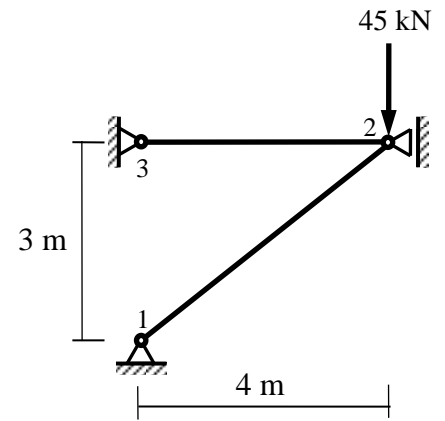
where, $\lambda = \cos \alpha$ and $\mu = \sin \alpha$

For the shown loaded truss, use **the stiffness method**

Given Data:

$E = 2.0 \times 10^7 \text{ kN/m}^2$ and $A = 5.0 \times 10^{-4} \text{ m}^2$

Choose the nearest answer.



36. The number of the non-zero DOF for the shown truss is:
 (A) Zero (B) 1 (C) 2 (D) 3
37. The terms (coefficients) of the force vector $\{F\}$ of the shown frame are:
 (A) $X_1, Y_1, X_2, -45, X_3, Y_3$ (B) $X_1, Y_1, 0, 0, X_3, Y_3$ (C) $X_1, Y_1, -54, X_2, X_3, Y_3$ (D) $X_1, Y_1, M_1, X_2, -45, X_3, Y_3, M_3$
38. The terms (coefficients) of the displacement vector of element 1 (nodes 1 & 2) are:
 (A) $0, 0, 0, v_2, 0, v_3$ (B) $0, v_1, 0, v_2$ (C) $0, 0, 0, 0$ (D) $0, 0, 0, v_2$
39. The terms (coefficients) of the displacement vector of element 2 (nodes 2 & 3) are:
 (A) $0, v_2, 0, 0$ (B) $0, 0, v_2, 0, 0, 0$ (C) $0, v_2, 0, 0, v_2$ (D) $0, v_1, 0, v_2$
40. The terms (coefficients) of the displacement vector $\{\Delta\}$ of the shown truss are:
 (A) $0, -45, 0, v_2, 0, 0, 0$ (B) $10, v_1, 0, v_2, 10, 0$ (C) $0, 0, 0, v_2, 0, 0$ (D) $0, 0, 0, v_2, 0, 0, v_2, 0$
41. The terms (coefficients) of the fixed end solution $\{F^f\}$ of the shown truss are:
 (A) $0, 0, -45, 0, 0, 0$ (B) $0, 0, -45, 0, 0, 0$ (C) $X_1, Y_1, 0, -45, 0, 0$ (D) There is no $\{F^f\}$ in truss
42. The properties of element 1 (nodes 1 & 2) are.
 (A) $\lambda = 0.8, \mu = 0.6, L = 3 \text{ m}$ (B) $\lambda = 0.8, \mu = 0.6, L = 5 \text{ m}$ (C) $\lambda = 0.8, \mu = 0.6, L = 4 \text{ m}$ (D) $\lambda = 0.8, \mu = 0, L = 5 \text{ m}$
43. The properties of element 2 (nodes 2 & 3) are.
 (A) $\lambda = -1, \mu = 0, L = 3 \text{ m}$ (B) $\lambda = -1, \mu = 0, L = 5 \text{ m}$ (C) $\lambda = -1, \mu = 0, L = 4 \text{ m}$ (D) $\lambda = -1, \mu = 0.8, L = 3 \text{ m}$
44. The terms (coefficients) of the fourth column of the stiffness matrix of element 1 (nodes 1 & 2) $[K^1]$ are:
 (A) $-960, -720, 960, 720$ (B) $-960, -720, 0, 0$ (C) $0, 0, 960, 720$ (D) $-960, 0, 0, 720$
45. The terms (coefficients) of the second column of the stiffness matrix of element 2 (nodes 2 & 3) $[K^2]$ are:
 (A) $-960, -720, 960, 720$ (B) $0, 0, 960, 720$ (C) $-960, -720, 0, 0$ (D) $0, 0, 0, 0$
46. The displacement v_2 at node 2 is:
 (A) $5.0 \text{ mm} \downarrow$ (B) $62.5 \text{ mm} \downarrow$ (C) $16.3 \text{ mm} \downarrow$ (D) zero
47. The value of the horizontal reaction at node 1 is:
 (A) zero (B) 60 kN (C) 45 kN (D) 22.5 kN
48. The values of the vertical reaction at node 1 is:
 (A) 60 kN (B) 45 kN (C) zero (D) 22.5 kN
49. The value of the horizontal reaction at node 2 is:
 (A) zero (B) 60 kN (C) 45 kN (D) 22.5 kN
50. The value of the horizontal reaction at node 3 is:
 (A) 60 kN (B) 45 kN (C) 22.5 kN (D) zero

$$[K_e] = \begin{bmatrix} \frac{EA}{L} \lambda^2 & \frac{EA}{L} \mu \lambda & -\frac{EA}{L} \lambda^2 & -\frac{EA}{L} \mu \lambda \\ \frac{EA}{L} \mu \lambda & \frac{EA}{L} \mu^2 & -\frac{EA}{L} \mu \lambda & -\frac{EA}{L} \mu^2 \\ -\frac{EA}{L} \lambda^2 & -\frac{EA}{L} \mu \lambda & \frac{EA}{L} \lambda^2 & \frac{EA}{L} \mu \lambda \\ -\frac{EA}{L} \mu \lambda & -\frac{EA}{L} \mu^2 & \frac{EA}{L} \mu \lambda & \frac{EA}{L} \mu^2 \end{bmatrix}$$

where, $\lambda = \cos \alpha$ and $\mu = \sin \alpha$

With my best wishes
Dr. M. Abdel-Kader