

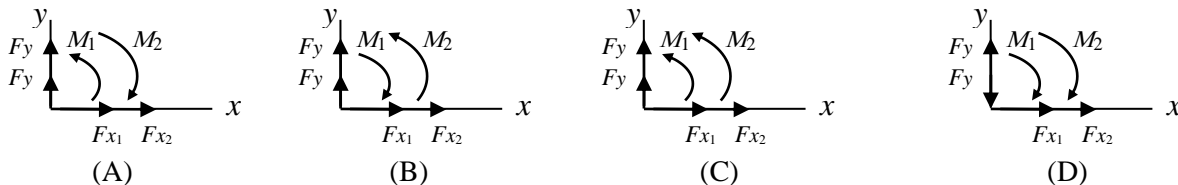
**Final Exam**

Total Marks: 75

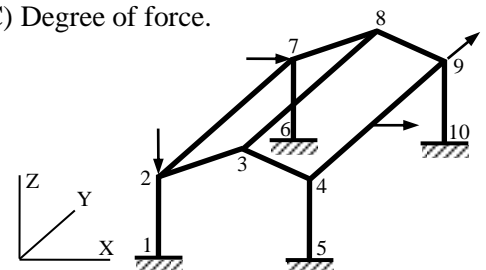
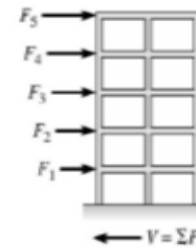
No. of Questions: 50 (Attempt all questions)

**Choose the nearest answer. (a2, a5, b1, b7, c1, c6)**

- Stiffness is the property of an element which is defined as:  
(A) Displacement per unit area. (B) Displacement per unit force. (C) Force per unit force.  
(D) Force per unit displacement.
- For plane frame element 1-2 (connecting joints 1 and 2), the positive sign of forces (forces and moments) is:



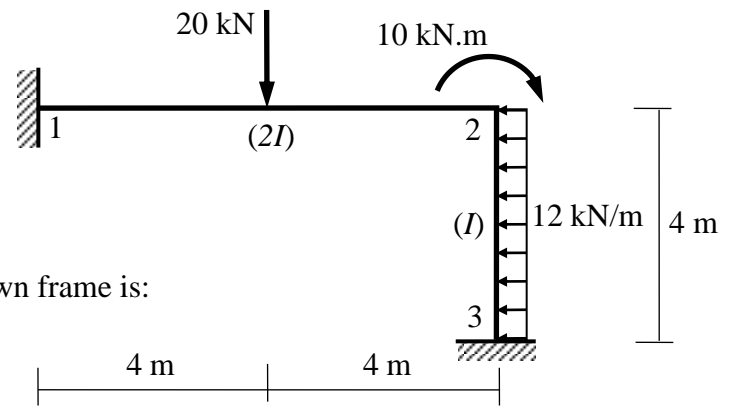
- One of the assumptions that the stiffness method is based on to analyze plane frames is:  
(A) Members will behave in non-linear and plastic manner.  
(B) Members (beams and columns) are straight with constant properties between joints.  
(C) Applied loads will act out of the structure plane.
- In SAP, loads and properties of material are:  
(A) Fixed data. (B) Output data. (C) Input data. (D) Results of the analysis.
- In SAP, the ..... must be defined for (1D) plane frame elements.  
(A) Areas (B) Thicknesses (C) Sections (D) Colors
- The horizontal forces applied on the shown frame is called ..... load.  
(A) Earth pressure (B) Earthquake (C) Settlement (D) Hydrostatic
- In SAP, the internal forces are:  
(A) Fixed data. (B) Input data. (C) Given data. (D) Output data.
- In SAP, self-weight loading always acts in the ... direction.  
(A) X (B) Y (C) -Y (D) -Z
- Wind load applied over the height of high-rise buildings is assumed:  
(A) Constant. (B) 1000 kN/m. (C) Perpendicular to the surface. (D) Parallel to the surface.
- When the material properties are independent of the coordinates, the material is:  
(A) Isotropic. (B) Non-linear. (C) Plastic. (D) Homogeneous.
- The responsibility of the analytical model results lies on:  
(A) The company developed the software. (B) The structural designer who developed the software.  
(C) The structural designer who used the software. (D) The computer used.
- The abbreviation "CAD" means:  
(A) Common Analysis Data. (B) Computer-Aided Design. (C) Calculation And Design. (D) Computer And Data.
- The abbreviation "DOF" means:  
(A) Possible translations at nodes. (B) Possible rotations at nodes. (C) Degree of force.  
(D) Possible translations and rotations at nodes.
- The number of non-zero DOF for the shown space frame is:  
(A) 60 (B) 30 (C) 36 (D) 18
- The number of non-zero DOF per node 1 in the shown space frame is:  
(A) Zero (B) 6 (C) 2 (D) 3
- The number of non-zero DOF per node 2 in the shown space frame is:  
(A) Zero (B) 3 (C) 4 (D) 6
- If the axial deformation is neglected, the number of non-zero DOF per node 2 in the shown space frame is:  
(A) 4 (B) 3 (C) 5 (D) 2
- When there are loads between the nodes, the equilibrium equation of a plane frame is  $\{F\} = [K]\{\Delta\} + \{F^f\}$  where;  
(A)  $\{F\}$  is the nodal forces. (B)  $\{F^f\}$  is the nodal displacements. (C)  $[F^f]$  is the element stiffness matrix.  
(D)  $\{\Delta\}$  is the nodal forces.
- In 2D Analysis, ..... can be used.  
(A) only 2D elements. (B) 1D, 2D and 3D elements. (C) 2D and 3D elements (D) 1D and 2D elements.
- Structures that cannot be modeled with the frame element are:  
(A) Space frames. (B) Space trusses. (C) Flat slabs. (D) Plane frames.



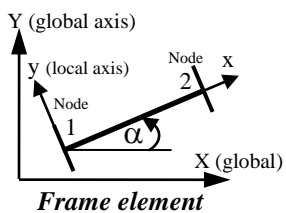
**Please turn over**

For the shown loaded plane frame with variable moment of inertia, use **the stiffness method** and **neglect axial deformation**:

Choose the nearest answer. (b1, b7, c1, c6)



21. The shown frame has ... nodes.  
(A) 1 (B) 2 (C) 3 (D) 4
22. The least number of elements to be taken for the shown frame is:  
(A) 1 (B) 2 (C) 3 (D) 4
23. By neglecting axial deformation, the number of the non-zero DOF for the shown frame becomes:  
(A) Zero (B) 1 (C) 2 (D) 3
24. The terms (coefficients) of the force vector  $\{F\}$  of the shown frame are:  
(A)  $X_1, Y_1, M_1, 0, 0, -10, X_3, Y_3, M_3$  (B)  $X_1, Y_1, M_1, 0, 20, 0, X_3, Y_3, M_3$  (C)  $X_1, Y_1, -20, 10, 20, 0, X_3, Y_3, M_1$
25. The terms (coefficients) of the displacement vector  $\{\Delta\}$  of the shown frame are:  
(A)  $0, 0, 0, u_2, v_2, \theta_2, 0, 0, 0$  (B)  $0, 0, 0, 0, 0, \theta_2, 0, 0, 0$  (C)  $0, 0, 0, \theta_2, 0, 0$  (D)  $0, 0, \theta_1, 0, 0, \theta_2, 0, 0, \theta_3$
26. The terms (coefficients) of the fixed end solution of element 1 (nodes 1 & 2) are:  
(A)  $0, 10, 20, 0, 10, -20$  (B)  $0, 20, 10, 20, 10, -20$  (C)  $10, 0, 20, 10, 0, -20$  (D)  $0, 0, 20, 0, 0, -20$
27. The properties of element 1 (nodes 1 & 2) are.  
(A)  $\alpha = 0, \lambda = 1, \mu = 0$  and  $L=8$  m (B)  $\alpha = 0, \lambda = 1, \mu = 0$  and  $L=4$  m (C)  $\alpha = 0, \lambda = 0, \mu = 1$  and  $L=8$  m
28. The terms (coefficients) of the sixth column of the stiffness matrix of element 1  $[K^1]$  are:  
(A)  $0, 3EI/16, EI/2, 0, -3EI/16, EI$  (B)  $0, 0, EI/2, 0, -3EI/6, EI$  (C)  $0, 0, EI/2, 0, -3EI, EI$
29. The rotation angle  $\theta_2$  at node 2 is:  
(A)  $-800/EI$  (B)  $-30/2EI$  (C)  $-3/EI$  (D)  $-40/3EI$
30. The final bending moment at node 1 is:  
(A)  $-1.5$  kN.m (B)  $8.0$  kN.m (C)  $-72.5$  kN.m (D)  $-18.5$  kN.m
31. The final bending moments at node 2 are:  
(A)  $40$  and  $30$  kN.m (B)  $-7$  and  $-20$  kN.m (C)  $-3$  and  $-13$  kN.m (D)  $-23$  and  $-13$  kN.m
32. The final bending moment at node 3 is:  
(A)  $-17.5$  kN.m (B)  $-17.5$  kN.cm (C)  $-17.5$  N.m (D)  $-17.5$  N.mm
33. The final bending moment at the middle of element 1 (nodes 1 & 2) is:  
(A)  $80.2$  kN.m (B)  $70.6$  kN.m (C)  $19.25$  kN.m (D)  $2.25$  kN.m
34. The final bending moment at the middle of element 2 (nodes 2 & 3) is:  
(A) zero (B)  $70.6$  kN.m (C)  $18.5$  kN.m (D)  $8.75$  kN.m
35. The final vertical reaction at node 1 is:  
(A)  $20.7$  kN (B)  $9.4$  kN (C)  $0.5$  kN (D)  $80.5$  kN



$$[K_e] = \begin{bmatrix} \left( \frac{EA}{L} \lambda^2 + \frac{12EI}{L^3} \mu^2 \right) & \left( \frac{EA}{L} \mu \lambda - \frac{12EI}{L^3} \mu \lambda \right) & -\frac{6EI}{L^2} \mu & \left( -\frac{EA}{L} \lambda^2 - \frac{12EI}{L^3} \mu^2 \right) & \left( -\frac{EA}{L} \mu \lambda + \frac{12EI}{L^3} \mu \lambda \right) & -\frac{6EI}{L^2} \mu \\ \left( \frac{EA}{L} \mu \lambda - \frac{12EI}{L^3} \mu \lambda \right) & \left( \frac{EA}{L} \mu^2 + \frac{12EI}{L^3} \lambda^2 \right) & \frac{6EI}{L^2} \lambda & \left( -\frac{EA}{L} \mu \lambda + \frac{12EI}{L^3} \mu \lambda \right) & \left( -\frac{EA}{L} \mu^2 - \frac{12EI}{L^3} \lambda^2 \right) & \frac{6EI}{L^2} \lambda \\ -\frac{6EI}{L^2} \mu & \frac{6EI}{L^2} \lambda & \frac{4EI}{L} & \frac{6EI}{L^2} \mu & -\frac{6EI}{L^2} \lambda & \frac{2EI}{L} \\ \left( -\frac{EA}{L} \lambda^2 - \frac{12EI}{L^3} \mu^2 \right) & \left( -\frac{EA}{L} \mu \lambda + \frac{12EI}{L^3} \mu \lambda \right) & \frac{6EI}{L^2} \mu & \left( \frac{EA}{L} \lambda^2 + \frac{12EI}{L^3} \mu^2 \right) & \left( \frac{EA}{L} \mu \lambda - \frac{12EI}{L^3} \mu \lambda \right) & \frac{6EI}{L^2} \mu \\ \left( -\frac{EA}{L} \mu \lambda + \frac{12EI}{L^3} \mu \lambda \right) & \left( -\frac{EA}{L} \mu^2 - \frac{12EI}{L^3} \lambda^2 \right) & -\frac{6EI}{L^2} \lambda & \left( \frac{EA}{L} \mu \lambda - \frac{12EI}{L^3} \mu \lambda \right) & \left( \frac{EA}{L} \mu^2 + \frac{12EI}{L^3} \lambda^2 \right) & -\frac{6EI}{L^2} \lambda \\ -\frac{6EI}{L^2} \mu & \frac{6EI}{L^2} \lambda & \frac{2EI}{L} & \frac{6EI}{L^2} \mu & -\frac{6EI}{L^2} \lambda & \frac{4EI}{L} \end{bmatrix}$$

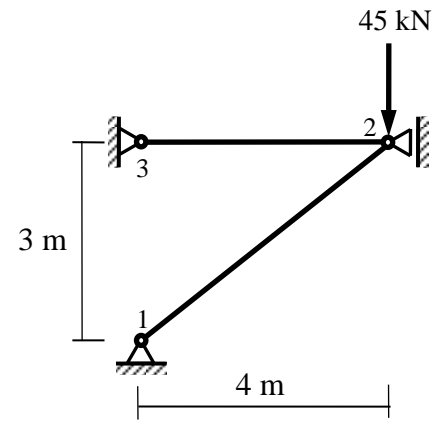
where,  $\lambda = \cos \alpha$  and  $\mu = \sin \alpha$

For the shown loaded truss, use **the stiffness method**

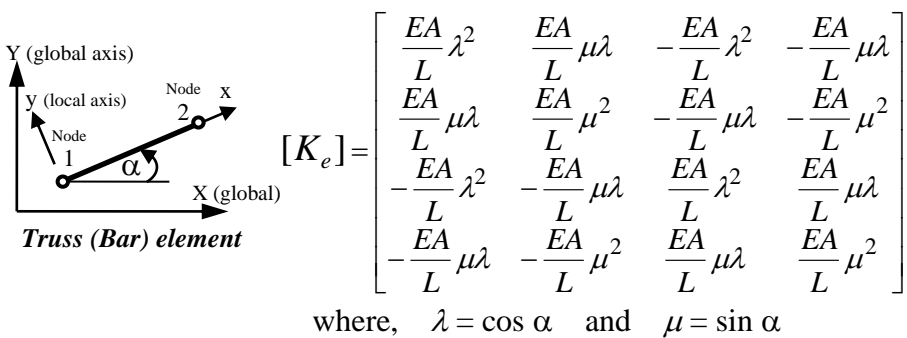
**Given Data:**

$E = 2.0 \times 10^7 \text{ kN/m}^2$  and  $A = 5.0 \times 10^{-4} \text{ m}^2$

Choose the nearest answer. (b1, b7, c1, c6)



36. The number of the non-zero DOF for the shown truss is:  
 (A) Zero (B) 1 (C) 2 (D) 3
37. The terms (coefficients) of the force vector  $\{F\}$  of the shown frame are:  
 (A)  $X_1, Y_1, X_2, -45, X_3, Y_3$  (B)  $X_1, Y_1, 0, 0, X_3, Y_3$  (C)  $X_1, Y_1, -54, X_2, X_3, Y_3$  (D)  $X_1, Y_1, M_1, X_2, -45, X_3, Y_3, M_3$
38. The terms (coefficients) of the displacement vector of element 1 (nodes 1 & 2) are:  
 (A)  $0, 0, 0, v_2, 0, v_3$  (B)  $0, v_1, 0, v_2$  (C)  $0, 0, 0, 0$  (D)  $0, 0, 0, v_2$
39. The terms (coefficients) of the displacement vector of element 2 (nodes 2 & 3) are:  
 (A)  $0, v_2, 0, 0$  (B)  $0, 0, v_2, 0, 0, 0$  (C)  $0, v_2, 0, 0, v_2$  (D)  $0, v_1, 0, v_2$
40. The terms (coefficients) of the displacement vector  $\{\Delta\}$  of the shown truss are:  
 (A)  $0, -45, 0, v_2, 0, 0, 0$  (B)  $10, v_1, 0, v_2, 10, 0$  (C)  $0, 0, 0, v_2, 0, 0$  (D)  $0, 0, 0, v_2, 0, 0, v_2, 0$
41. The terms (coefficients) of the fixed end solution  $\{F^f\}$  of the shown truss are:  
 (A)  $0, 0, -45, 0, 0, 0$  (B)  $0, 0, -45, 0, 0, 0$  (C)  $X_1, Y_1, 0, -45, 0, 0$  (D) There is no  $\{F^f\}$  in truss
42. The properties of element 1 (nodes 1 & 2) are.  
 (A)  $\lambda = 0.8, \mu = 0.6, L=3 \text{ m}$  (B)  $\lambda = 0.8, \mu = 0.6, L=5 \text{ m}$  (C)  $\lambda = 0.8, \mu = 0.6, L=4 \text{ m}$  (D)  $\lambda = 0.8, \mu = 0, L=5 \text{ m}$
43. The properties of element 2 (nodes 2 & 3) are.  
 (A)  $\lambda = -1, \mu = 0, L=3 \text{ m}$  (B)  $\lambda = -1, \mu = 0, L=5 \text{ m}$  (C)  $\lambda = -1, \mu = 0, L=4 \text{ m}$  (D)  $\lambda = -1, \mu = 0.8, L=3 \text{ m}$
44. The terms (coefficients) of the fourth column of the stiffness matrix of element 1 (nodes 1 & 2)  $[K^1]$  are:  
 (A)  $-960, -720, 960, 720$  (B)  $-960, -720, 0, 0$  (C)  $0, 0, 960, 720$  (D)  $-960, 0, 0, 720$
45. The terms (coefficients) of the second column of the stiffness matrix of element 2 (nodes 2 & 3)  $[K^2]$  are:  
 (A)  $-960, -720, 960, 720$  (B)  $0, 0, 960, 720$  (C)  $-960, -720, 0, 0$  (D)  $0, 0, 0, 0$
46. The displacement  $v_2$  at node 2 is:  
 (A)  $5.0 \text{ mm} \downarrow$  (B)  $62.5 \text{ mm} \downarrow$  (C)  $16.3 \text{ mm} \downarrow$  (D) zero
47. The value of the horizontal reaction at node 1 is:  
 (A) zero (B)  $60 \text{ kN}$  (C)  $45 \text{ kN}$  (D)  $22.5 \text{ kN}$
48. The values of the vertical reaction at node 1 is:  
 (A)  $60 \text{ kN}$  (B)  $45 \text{ kN}$  (C) zero (D)  $22.5 \text{ kN}$
49. The value of the horizontal reaction at node 2 is:  
 (A) zero (B)  $60 \text{ kN}$  (C)  $45 \text{ kN}$  (D)  $22.5 \text{ kN}$
50. The value of the horizontal reaction at node 3 is:  
 (A)  $60 \text{ kN}$  (B)  $45 \text{ kN}$  (C)  $22.5 \text{ kN}$  (D) zero



With my best wishes  
**Dr. M. Abdel-Kader**