

## Final Exam

Total Marks: **60**

No. of Questions: **3** (Attempt all questions)

### Question (1): (20 Marks) (a2, a5)

(a) Choose the correct answer (Put **a, b, c** or **d** in front of the statement number in your answer paper).

1. In structural analysis programs, properties of material and loads are considered as
  - a) Results of the analysis.
  - b) Output data.
  - c) Input data.
  - d) Always not required in the analysis.
2. The responsibility of the analytical model results lies on
  - a) The structural designer who used the software.
  - b) The company developed the software.
  - c) The input data.
  - d) The computer used.
3. Stiffness is the property of an element which is defined as
  - a) Displacement per unit area.
  - b) Displacement per unit force.
  - c) Force per unit mass.
  - d) Force per unit displacement.
4. The correct choice of modeling and analysis tools/methods depends on
  - a) Importance of the structure.
  - b) Required level of response accuracy.
  - c) Purpose of structural analysis.
  - d) All the above.
5. For plane frame in X-Z plane, the fixed support has restraints in Joint Local Directions as:

Restraints in Joint Local Directions			
<input checked="" type="checkbox"/> Translation 1	<input checked="" type="checkbox"/> Rotation about 1		
<input type="checkbox"/> Translation 2	<input type="checkbox"/> Rotation about 2		
<input checked="" type="checkbox"/> Translation 3	<input checked="" type="checkbox"/> Rotation about 3		

a)

Restraints in Joint Local Directions			
<input checked="" type="checkbox"/> Translation 1	<input type="checkbox"/> Rotation about 1		
<input type="checkbox"/> Translation 2	<input checked="" type="checkbox"/> Rotation about 2		
<input checked="" type="checkbox"/> Translation 3	<input type="checkbox"/> Rotation about 3		

b)

Restraints in Joint Local Directions			
<input checked="" type="checkbox"/> Translation 1	<input type="checkbox"/> Rotation about 1		
<input checked="" type="checkbox"/> Translation 2	<input type="checkbox"/> Rotation about 2		
<input type="checkbox"/> Translation 3	<input checked="" type="checkbox"/> Rotation about 3		

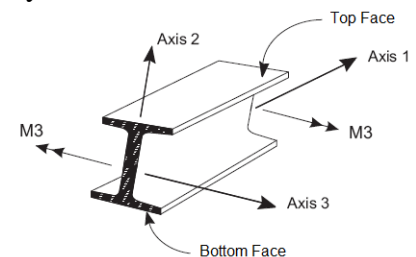
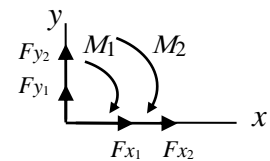
c)

Restraints in Joint Local Directions			
<input type="checkbox"/> Translation 1	<input type="checkbox"/> Rotation about 1		
<input type="checkbox"/> Translation 2	<input type="checkbox"/> Rotation about 2		
<input checked="" type="checkbox"/> Translation 3	<input type="checkbox"/> Rotation about 3		

d)

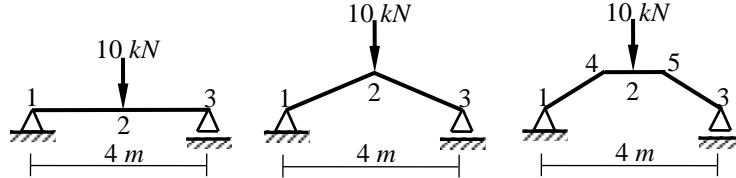
(b) **TRUE** or **FALSE** (Put  $\checkmark$  or  $\times$  in front of the statement number in your answer paper)

1. For plane frame element 1-2 (connecting joints 1 and 2), the positive sign of forces (forces and moments) is as shown in the figure.
2. The frame element is also called beam-column element.
3. For intermediate hinge, only the compatibility of the displacement is satisfied while the compatibility is not satisfied for the rotation.
4. The abbreviation "CAD" means Computer-Aided Design and the abbreviation "DOF" means Degree of Freedom.
5. In space frames, there are 6 DOF per free node, which are 3 translations and 3 rotations.
6. Bar element used in modeling trusses has two nodes at its ends, every node has 3 DOF in the element axial direction.
7. If the direction of the moment  $M_3$  is as shown in the figure, the top face will be subject to a tension.
8. Structures that can be modeled with the frame element include: 3-D and planar frames – 3-D and planar trusses – Flat slabs – Raft foundation.
9. The order of the input data: Editing Supports & Assigning Frame Sections is very important
10. Wind load is usually applied parallel to the surface.
11. In 2-D Analysis, 1D, 2D and 3D elements can be used.
12. For (2D) area elements, the sections must be defined.
13. For (1D) frame elements, the sections must be defined.



**Please turn over**

14. The bending moments at mid-span (at node 2) of the three beams shown below are the same ( $= 10 \text{ kN.m}$ ).



15. In the three beams shown above, when the axial deformation is neglected,  $u_3 = 0$  for the first beam only.

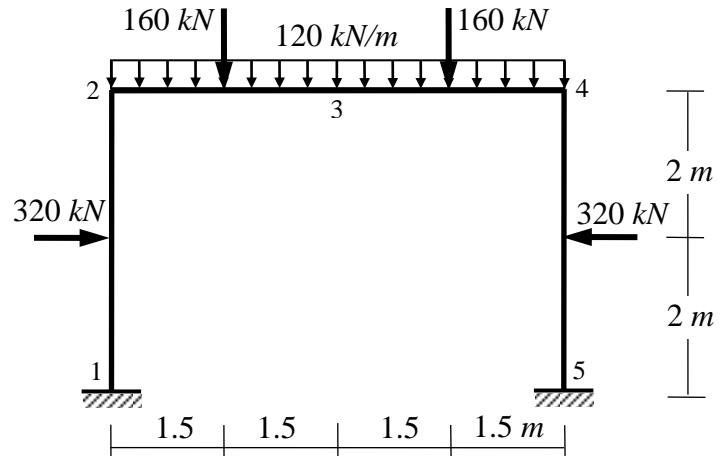
**Question (2): (20 Marks) (b1, b7, c1, c6)**

For the shown frame, using the stiffness method:  
Neglect axial deformation

- (a) Determine the displacements at the nodes due to the given load.
- (b) Draw the bending moment diagram.

**Given Data:**

$$E = 2.1 \times 10^7 \text{ kN/m}^2 \quad A = 0.15 \text{ m}^2 \quad I = 3.125 \times 10^{-3} \text{ m}^4$$



$$[K_e] = \begin{bmatrix} \left( \frac{EA}{L} \lambda^2 + \frac{12EI}{L^3} \mu^2 \right) & \left( \frac{EA}{L} \mu \lambda - \frac{12EI}{L^3} \mu \lambda \right) & -\frac{6EI}{L^2} \mu & \left( -\frac{EA}{L} \lambda^2 - \frac{12EI}{L^3} \mu^2 \right) & \left( -\frac{EA}{L} \mu \lambda + \frac{12EI}{L^3} \mu \lambda \right) & -\frac{6EI}{L^2} \mu \\ \left( \frac{EA}{L} \mu \lambda - \frac{12EI}{L^3} \mu \lambda \right) & \left( \frac{EA}{L} \mu^2 + \frac{12EI}{L^3} \lambda^2 \right) & \frac{6EI}{L^2} \lambda & \left( -\frac{EA}{L} \mu \lambda + \frac{12EI}{L^3} \mu \lambda \right) & \left( -\frac{EA}{L} \mu^2 - \frac{12EI}{L^3} \lambda^2 \right) & \frac{6EI}{L^2} \lambda \\ -\frac{6EI}{L^2} \mu & \frac{6EI}{L^2} \lambda & \frac{4EI}{L} & \frac{6EI}{L^2} \mu & -\frac{6EI}{L^2} \lambda & \frac{2EI}{L} \\ \left( -\frac{EA}{L} \lambda^2 - \frac{12EI}{L^3} \mu^2 \right) & \left( -\frac{EA}{L} \mu \lambda + \frac{12EI}{L^3} \mu \lambda \right) & \frac{6EI}{L^2} \mu & \left( \frac{EA}{L} \lambda^2 + \frac{12EI}{L^3} \mu^2 \right) & \left( \frac{EA}{L} \mu \lambda - \frac{12EI}{L^3} \mu \lambda \right) & \frac{6EI}{L^2} \mu \\ \left( -\frac{EA}{L} \mu \lambda + \frac{12EI}{L^3} \mu \lambda \right) & \left( -\frac{EA}{L} \mu^2 - \frac{12EI}{L^3} \lambda^2 \right) & -\frac{6EI}{L^2} \lambda & \left( \frac{EA}{L} \mu \lambda - \frac{12EI}{L^3} \mu \lambda \right) & \left( \frac{EA}{L} \mu^2 + \frac{12EI}{L^3} \lambda^2 \right) & -\frac{6EI}{L^2} \lambda \\ -\frac{6EI}{L^2} \mu & \frac{6EI}{L^2} \lambda & \frac{2EI}{L} & \frac{6EI}{L^2} \mu & -\frac{6EI}{L^2} \lambda & \frac{4EI}{L} \end{bmatrix}$$

Where,  $\lambda = \cos \alpha$  and  $\mu = \sin \alpha$

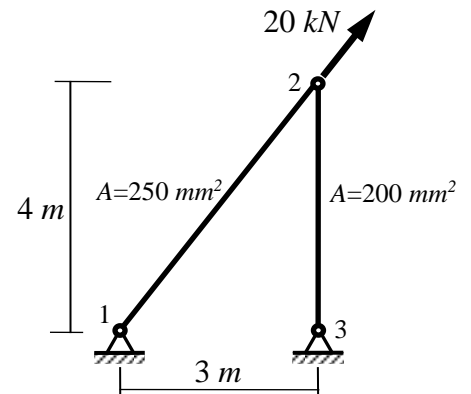
**Question (3): (20 Marks) (b1, b7, c1, c6)**

For the shown truss, using the stiffness method:

- (a) Determine the displacements at the nodes due to the given load.
- (b) Determine the reactions at the supports.

**Given Data:**

$E = 2.0 \times 10^7 \text{ kN/m}^2$ .  
A for each member is as shown on the truss.



$$[K_e] = \begin{bmatrix} \frac{EA}{L} \lambda^2 & \frac{EA}{L} \mu \lambda & -\frac{EA}{L} \lambda^2 & -\frac{EA}{L} \mu \lambda \\ \frac{EA}{L} \mu \lambda & \frac{EA}{L} \mu^2 & -\frac{EA}{L} \mu \lambda & -\frac{EA}{L} \mu^2 \\ -\frac{EA}{L} \lambda^2 & -\frac{EA}{L} \mu \lambda & \frac{EA}{L} \lambda^2 & \frac{EA}{L} \mu \lambda \\ -\frac{EA}{L} \mu \lambda & -\frac{EA}{L} \mu^2 & \frac{EA}{L} \mu \lambda & \frac{EA}{L} \mu^2 \end{bmatrix}$$

Where,  $\lambda = \cos \alpha$  and  $\mu = \sin \alpha$

With my best wishes

Dr. M. Abdel-Kader